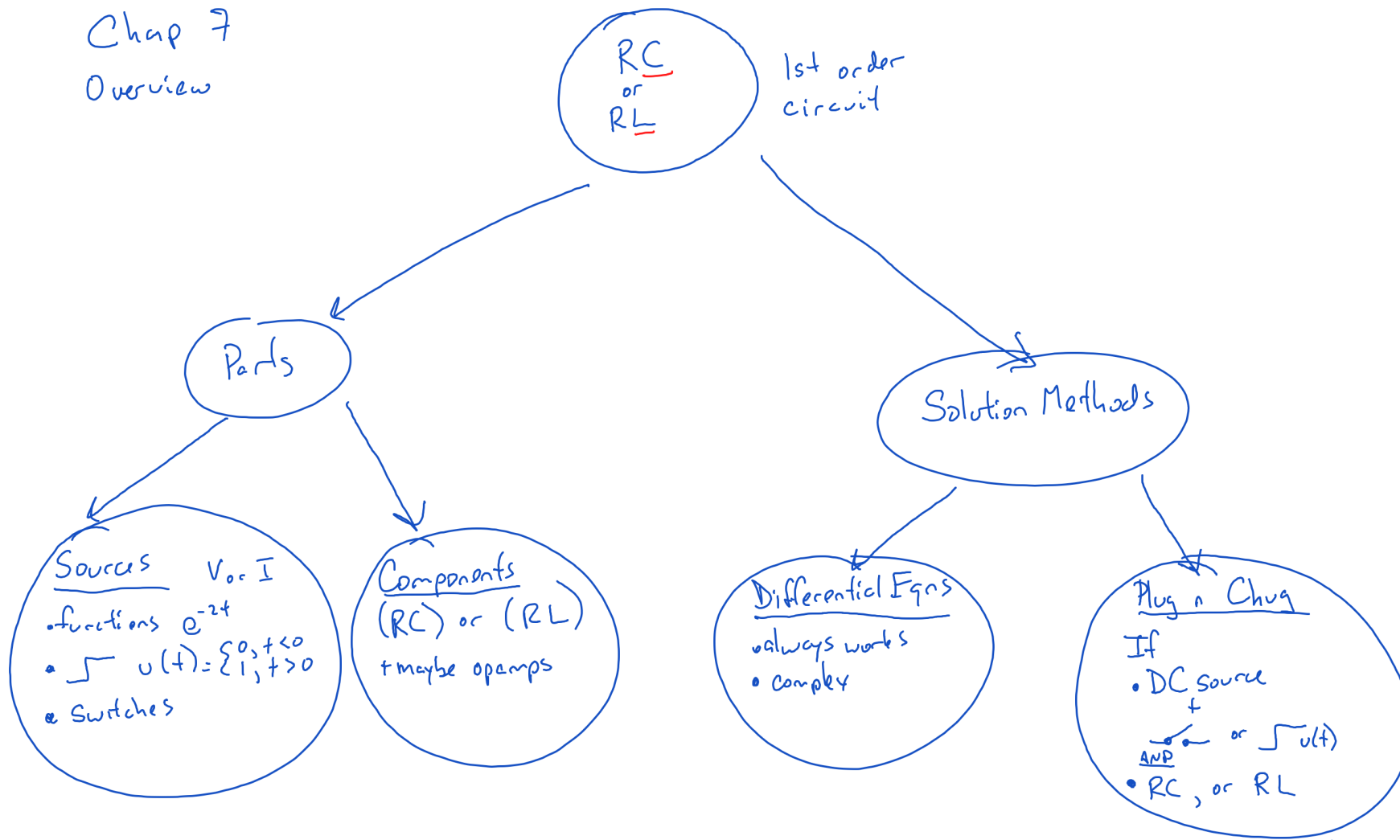
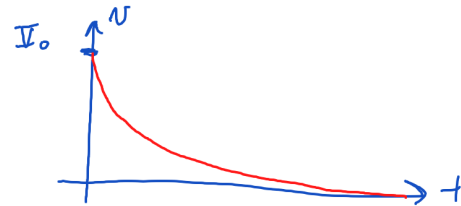
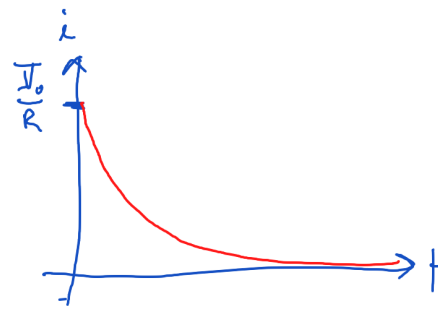
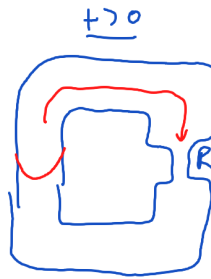
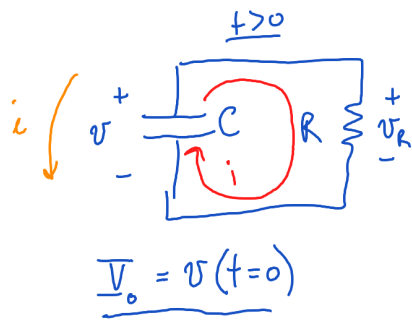


Chap 7

Overview



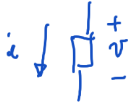
RC natural response



① Find DE in v

→ • $v_R = iR$ ←

→ • $i = C v_C' ←$



Passive

• KVL: $-v + v_R = 0$ ← geometry

$-v + iR = 0$ R

• $-v + C v' R = 0$ C

$-v'RC - v = 0$

$v' + \frac{1}{RC} v = 0$

$v(0) = V_0$

② Solve DE

• natural part $\left. \begin{matrix} s + \frac{1}{RC} = 0 \\ s = -\frac{1}{RC} \end{matrix} \right\} v_{nat}(t) = k e^{-\frac{1}{RC}t}$

• forced part 0

• total part

$v(t) = k e^{-\frac{1}{RC}t}$

$v(0) = V_0 = k$

total solution: $v(t) = V_0 e^{-\frac{1}{RC}t} = V_0 e^{-\frac{t}{\tau}}$ where $\tau = RC$

RC "time constant"
units seconds

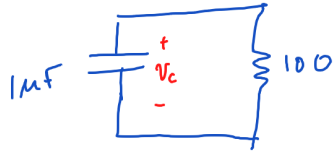
Plug-n-chug!

τ

• very quick (but approx) understanding of time to discharge

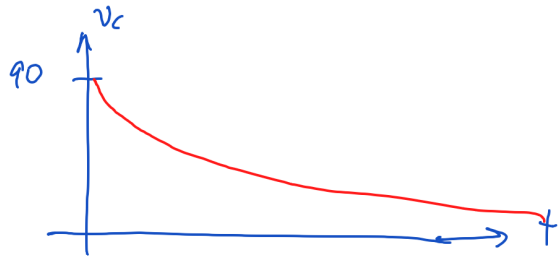
• $v(t) = V_0 e^{-\frac{t}{\tau}}$, $\tau = RC$

Ex



$v_c(0) = 90V$

$v_c(t) = 90 e^{-\frac{t}{\tau}}$, $\tau = (1m)(100) = 100\mu s$



Exact

when is it $\frac{1}{2}$ discharged?

$45 = 90 e^{-\frac{t}{100\mu s}}$

$\ln(\frac{1}{2}) = \ln(e^{-\frac{t}{10000}})$

$\ln(\frac{1}{2}) = -\frac{t}{10000}$

when is it 99% discharged?

$0.9 = 90 e^{-\frac{t}{100\mu s}}$...

$\frac{1}{100\mu} = \frac{1}{100} \cdot \frac{1}{m}$
 $= (0.01)M$
 $= 10k$

G
M
k
M
n
p

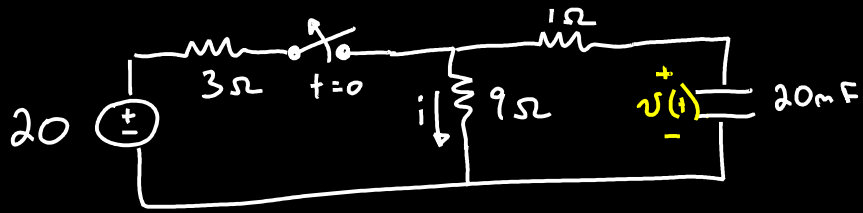
τ

"little less than τ " $e^{-1} \approx 0.35$

100 μs

"99% discharged at 5τ " 500 μs

First Order Problem



Find i for all time

① $V_o = v_c(t=0) : t < 0 = \boxed{15V}$

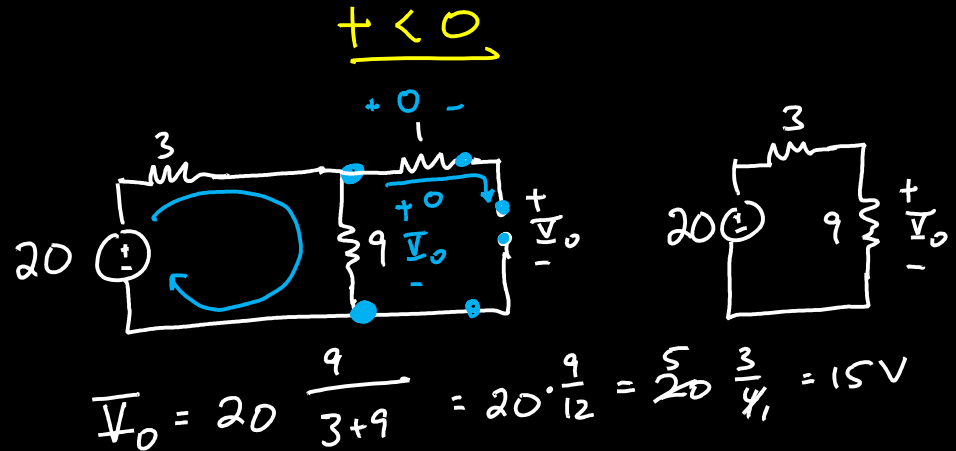
② τ

③ V_∞

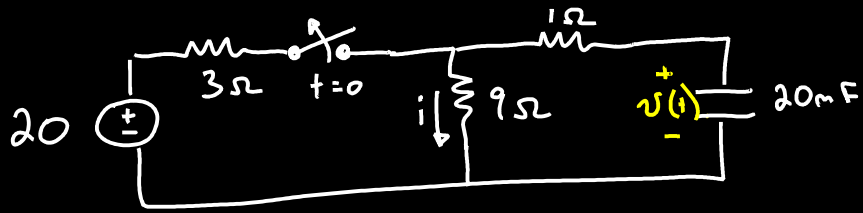
④ $v(t) = V_\infty + (V_o - V_\infty) e^{-t/\tau}$

⑤ $i(t)$

⑥ All time



First Order Problem



Find i for all time

① $V_o = v_c(t \leq 0) : t < 0 = \boxed{15V}$

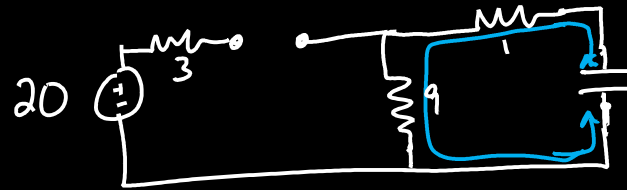
② $\tau : 0 < t < \infty = \boxed{\frac{1}{5} s}$

③ V_∞

④ $v(t) = V_\infty + (V_o - V_\infty) e^{-t/\tau}$

⑤ $i(t)$

⑥ All time



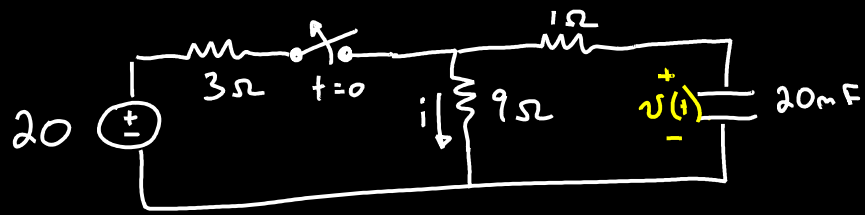
$R_{eq} = 1 + 9 = 10 \Omega$

$C = 20mF$

$\tau = RC$
 $= (10)(20m)$

$= 200m$
 $= \boxed{\frac{1}{5} s}$

First Order Problem



Find i for all time

① $V_o = v_c(t \leq 0) : t < 0 = \boxed{15V}$

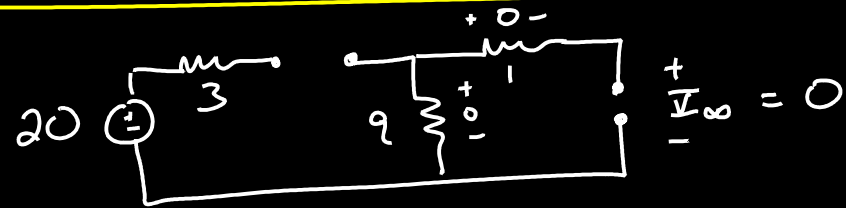
② $\tau : 0 < t < \infty = \boxed{\frac{1}{5} s}$

③ $V_\infty = v_c(t = \infty) : t = \infty = \boxed{0V}$

④ $v(t) = V_\infty + (V_o - V_\infty) e^{-t/\tau}$

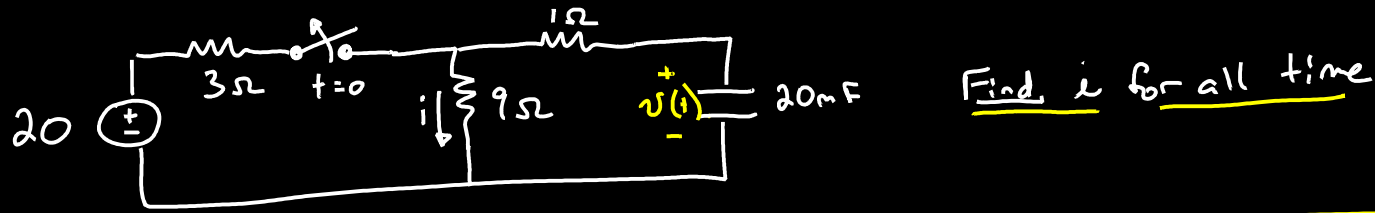
⑤ $i(t)$

⑥ All time



no switches
no cap, inductors
no $v(t)$

First Order Problem



① $V_o = v_c(t=0) : t < 0 = \boxed{15V}$

② $\tau : 0 < t < \infty = \boxed{\frac{1}{5} s}$

③ $V_\infty = v_c(t=\infty) : t = \infty = \boxed{0V}$

④ $v_c(t) = V_\infty + (V_o - V_\infty) e^{-t/\tau} = \begin{cases} 15, & t < 0 \\ \boxed{15e^{-5t} V}, & t \geq 0 \end{cases}$

⑤ $i(t) = \begin{cases} \frac{20}{3} A, & t < 0 \\ \boxed{1.5e^{-5t} A}, & t \geq 0 \end{cases}$

⑥ All time

$t > 0$

$$i(t) = \frac{v(t)}{R} = \frac{15e^{-5t}}{10} = \boxed{1.5e^{-5t} A}$$

$t < 0$

$$i = \frac{20}{3+9} = \frac{20}{12} = \frac{5}{3}$$